

Principles of  
**Microeconomics**  
Sixth Edition

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**Chapter : The Costs of Taxation**

In this chapter, look for the answers to these questions:

- How does a tax affect consumer surplus, producer surplus, and total surplus?
- What is the *deadweight loss* of a tax?
- What factors determine the size of this deadweight loss?
- How does tax revenue depend on the size of the tax?

# General overview of Tax

- A tax is a wedge between the price buyers pay and the price sellers receive.
- A tax raises the price buyers pay and lowers the price sellers receive.
- A tax reduces the quantity bought & sold.
- These effects are the same whether the tax is imposed on buyers or sellers, so we do not make this distinction in this chapter.

# The Effects of a Tax

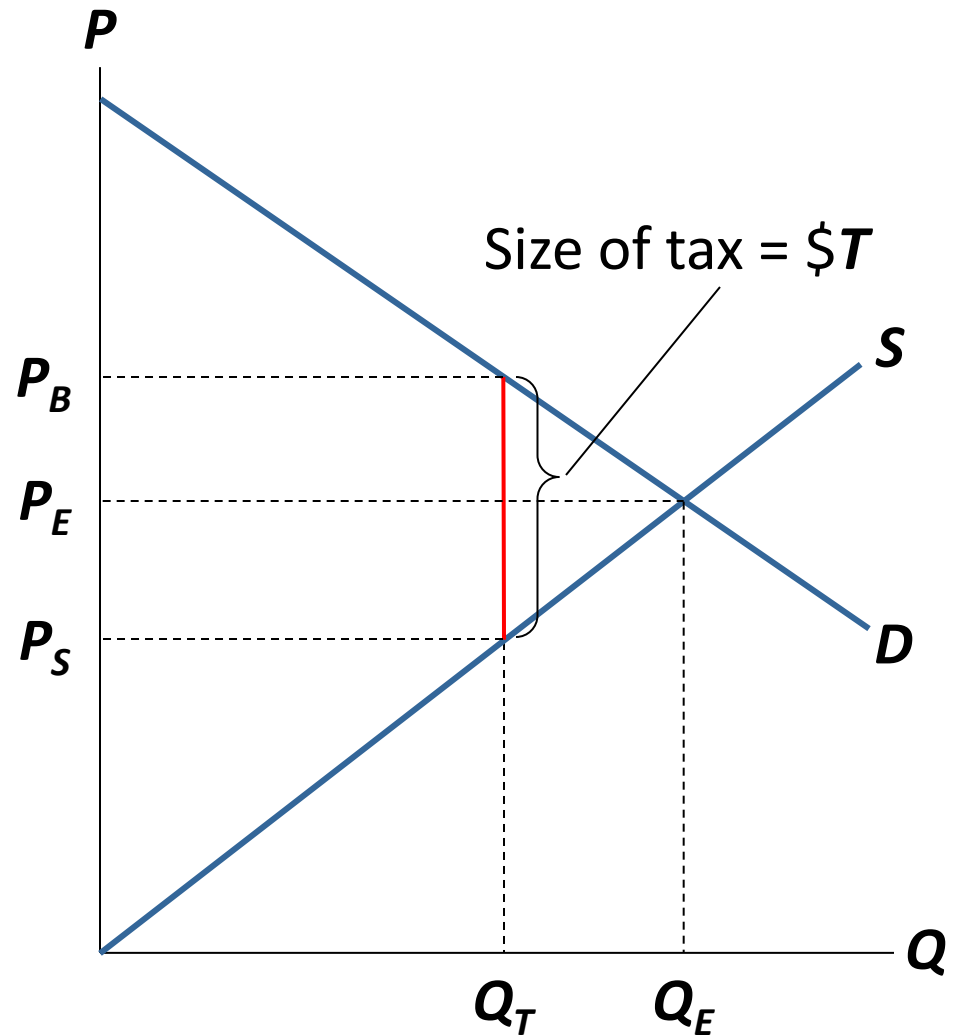
With no tax,  
eq'm price is  $P_E$  and  
quantity is  $Q_E$ .

Govt imposes a tax  
of  $\$T$  per unit.

The price buyers  
pay is  $P_B$ ,

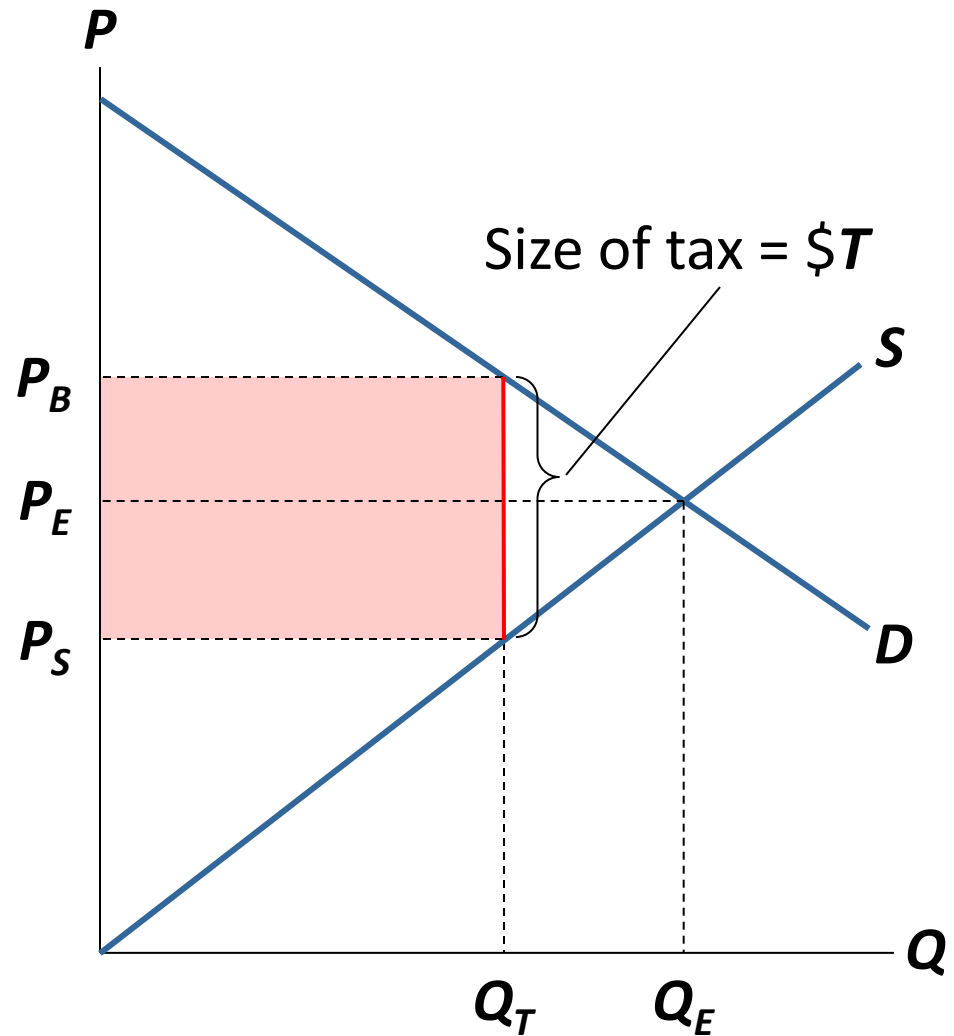
the price sellers  
receive is  $P_S$ ,

and quantity is  $Q_T$ .



# The Effects of a Tax

The tax generates revenue equal to  $\$T \times Q_T$ .



# The Effects of a Tax

- Next, we use the tools of welfare economics to measure the gains and losses from a tax.
- We will determine consumer surplus (CS), producer surplus (PS), tax revenue, and total surplus with and without the tax.
- Tax revenue is included in total surplus, because tax revenue can be used to provide services such as roads, police, public education, etc.

# The Effects of a Tax

Without a tax,

$$CS = A + B + C$$

$$PS = D + E + F$$

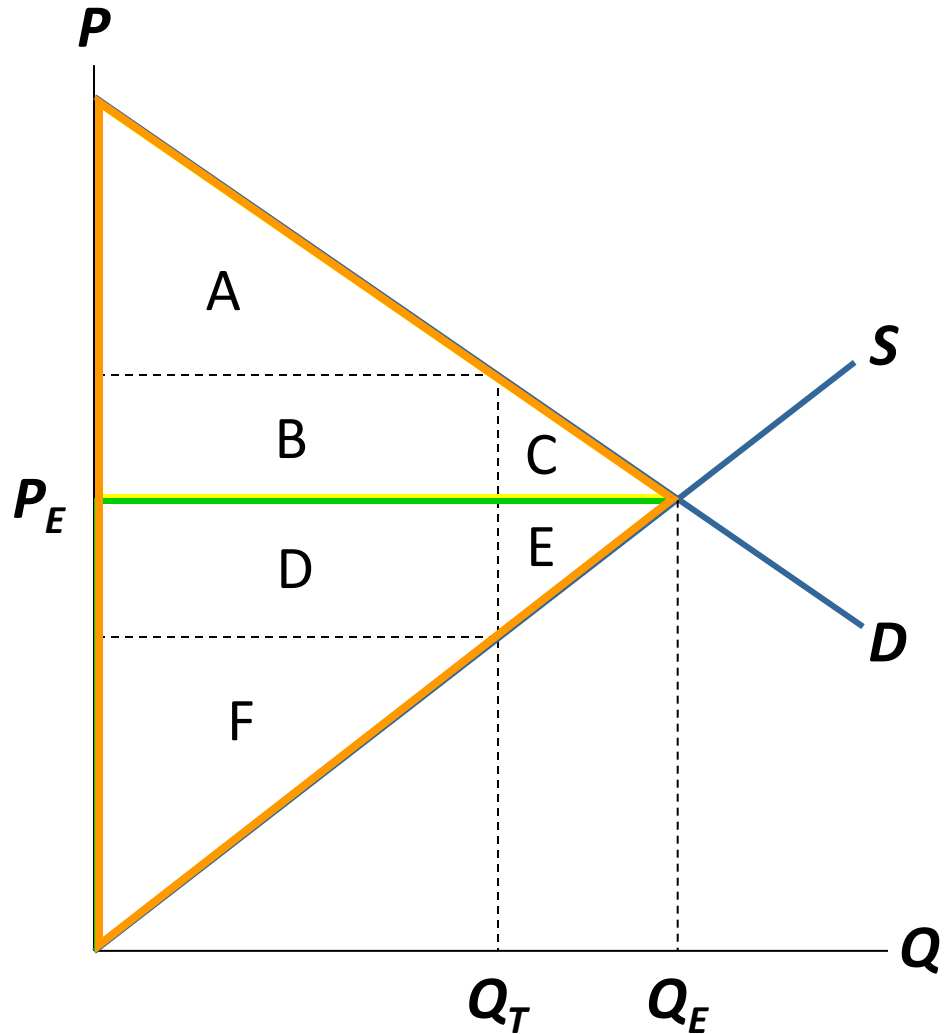
Tax revenue = 0

Total surplus

$$= CS + PS$$

$$= A + B + C$$

$$+ D + E + F$$



# The Effects of a Tax

With the tax,

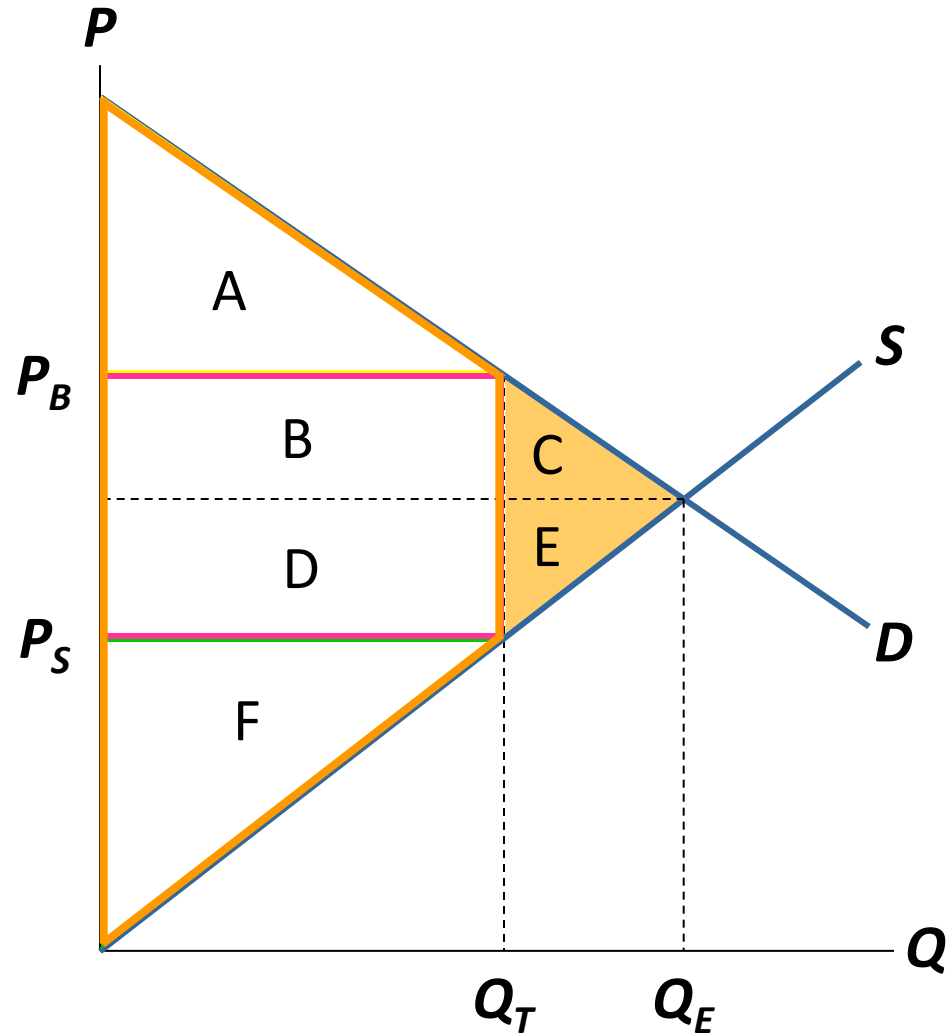
$$CS = A$$

$$PS = F$$

$$\begin{aligned} \text{Tax revenue} \\ = B + D \end{aligned}$$

$$\begin{aligned} \text{Total surplus} \\ = A + B \\ + D + F \end{aligned}$$

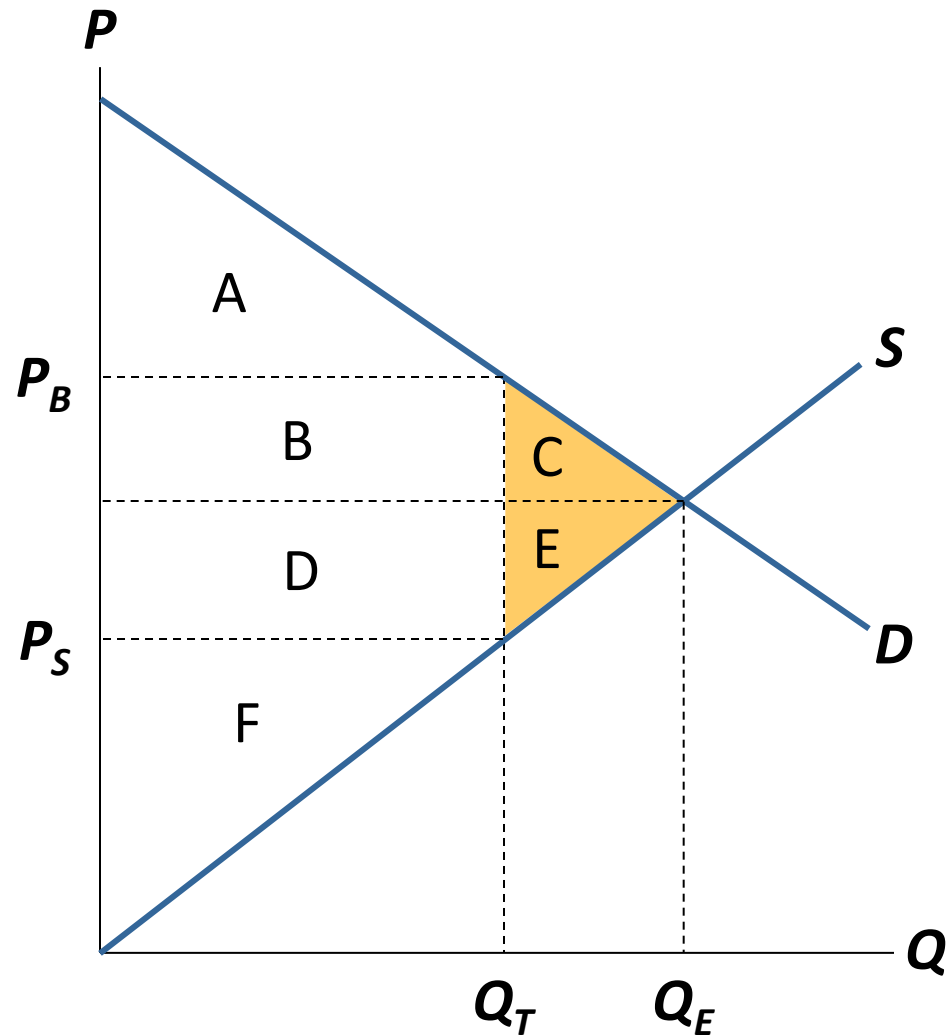
The tax causes  
total surplus to  
fall by  $C + E$





# The Effects of a Tax

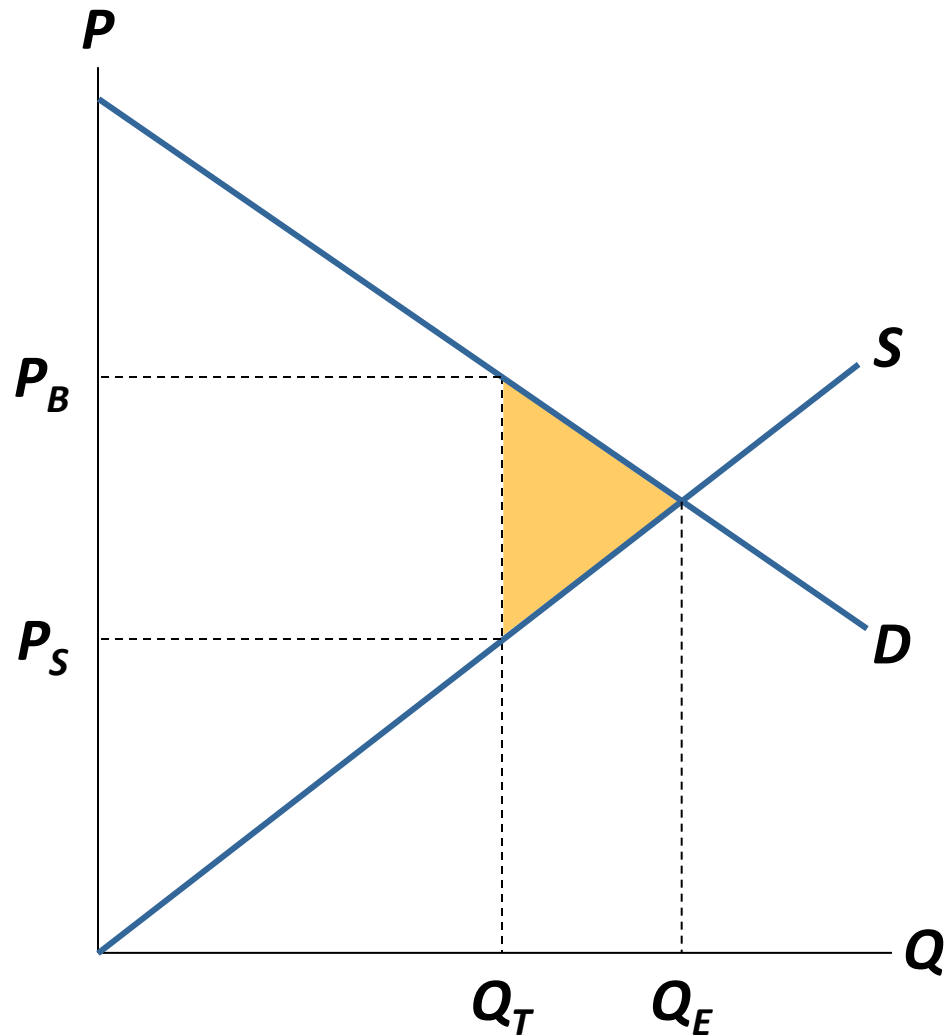
C + E is called the **deadweight loss** (DWL) of the tax, the fall in total surplus that results from a market distortion, such as a tax.



# About the Deadweight Loss

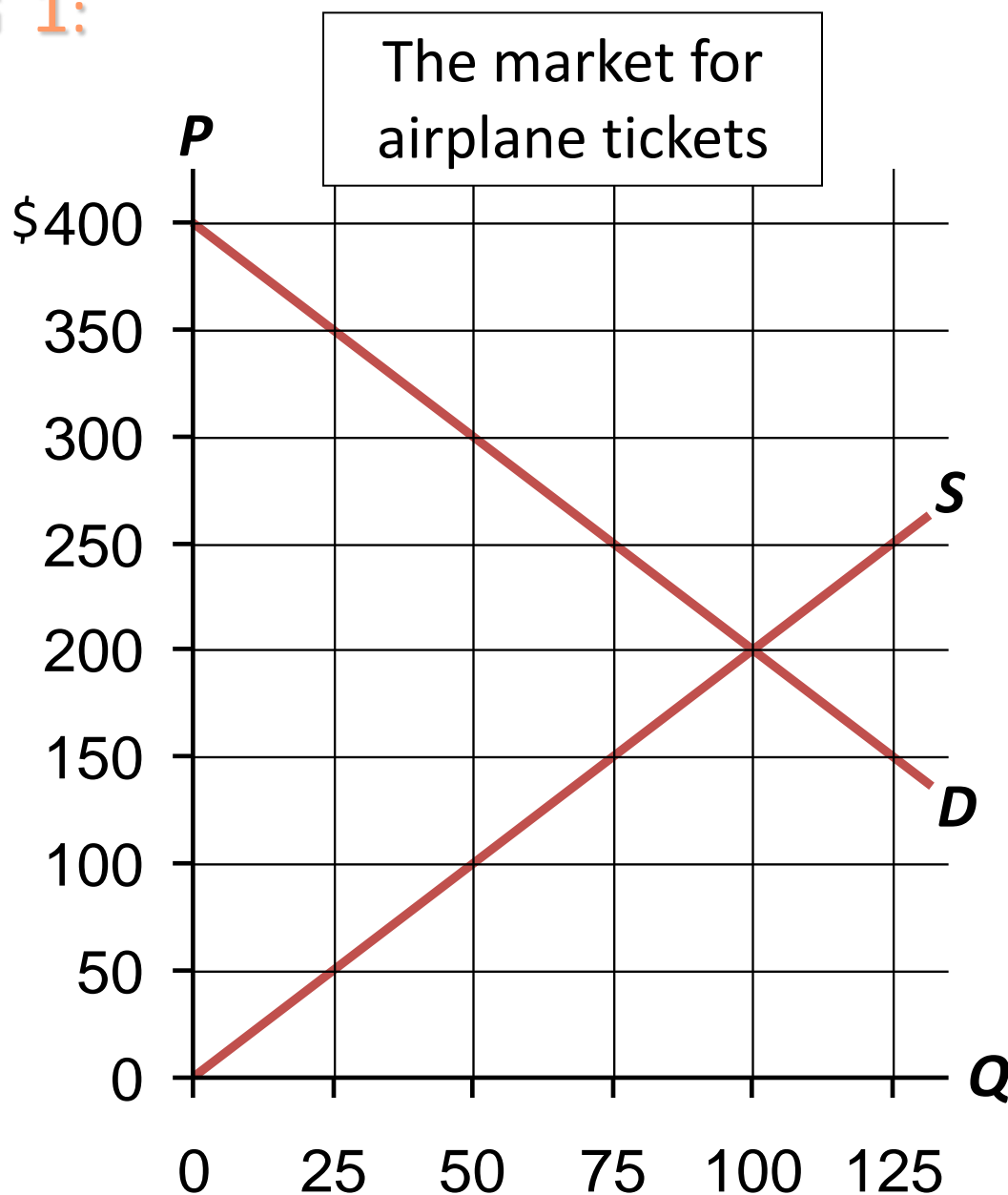
Because of the tax, the units between  $Q_T$  and  $Q_E$  are not sold.

The value of these units to buyers is greater than the cost of producing them, so the tax has prevented some mutually beneficial trades.



## ACTIVE LEARNING 1: Analysis of tax

- A. Compute CS, PS, and total surplus without a tax.
- B. If \$100 tax per ticket, compute CS, PS, tax revenue, total surplus, and DWL.



## ACTIVE LEARNING 1: Answers to A

CS

$$= \frac{1}{2} \times \$200 \times 100$$

$$= \underline{\$10,000}$$

PS

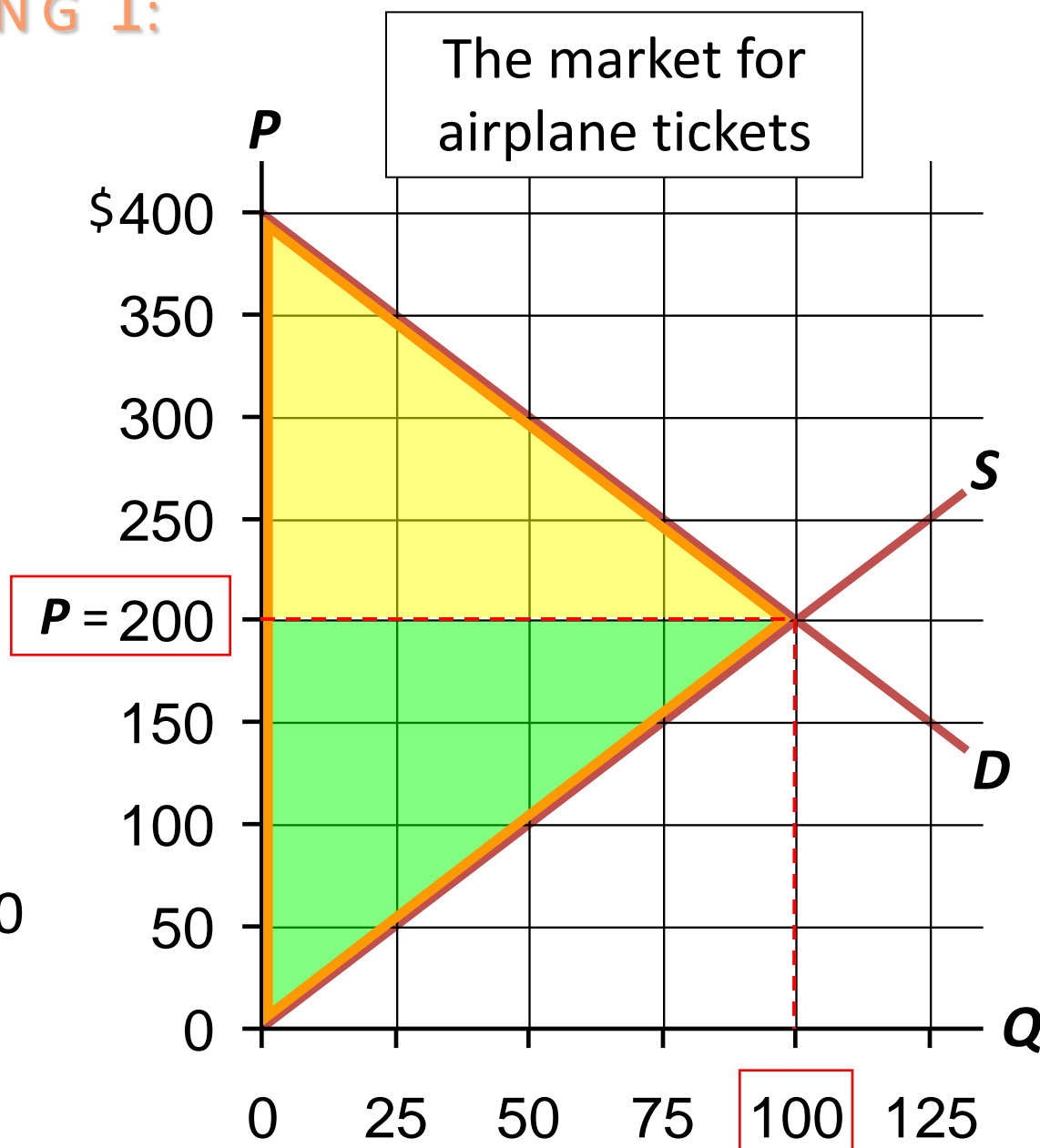
$$= \frac{1}{2} \times \$200 \times 100$$

$$= \underline{\$10,000}$$

total surplus

$$= \$10,000 + \$10,000$$

$$= \underline{\$20,000}$$



## ACTIVE LEARNING 1: Answers to B

CS

$$= \frac{1}{2} \times \$150 \times 75$$

$$= \underline{\$5,625}$$

$$PS = \underline{\$5,625}$$

tax revenue

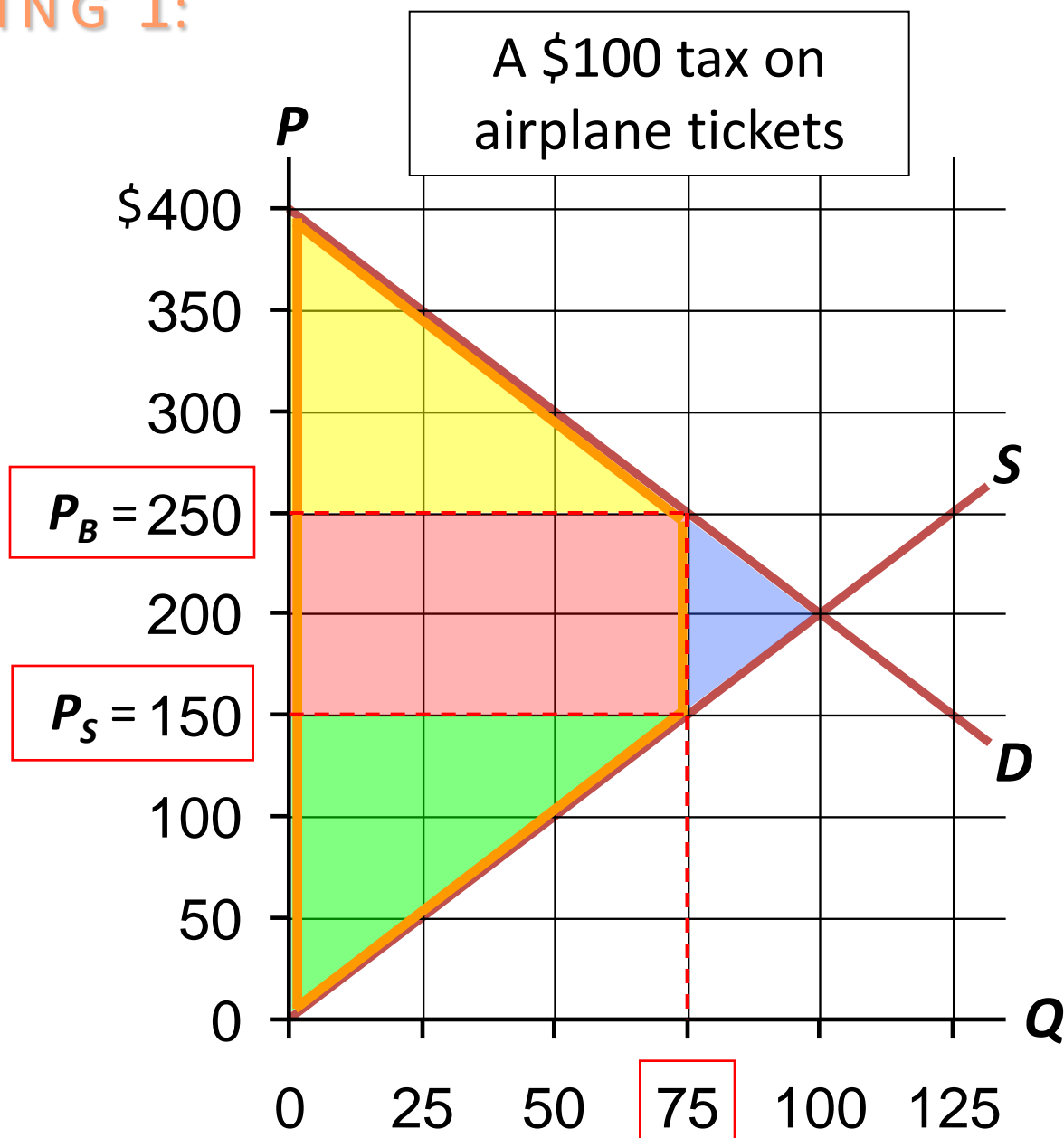
$$= \$100 \times 75$$

$$= \underline{\$7,500}$$

total surplus

$$= \underline{\$18,750}$$

$$DWL = \underline{\$1,250}$$

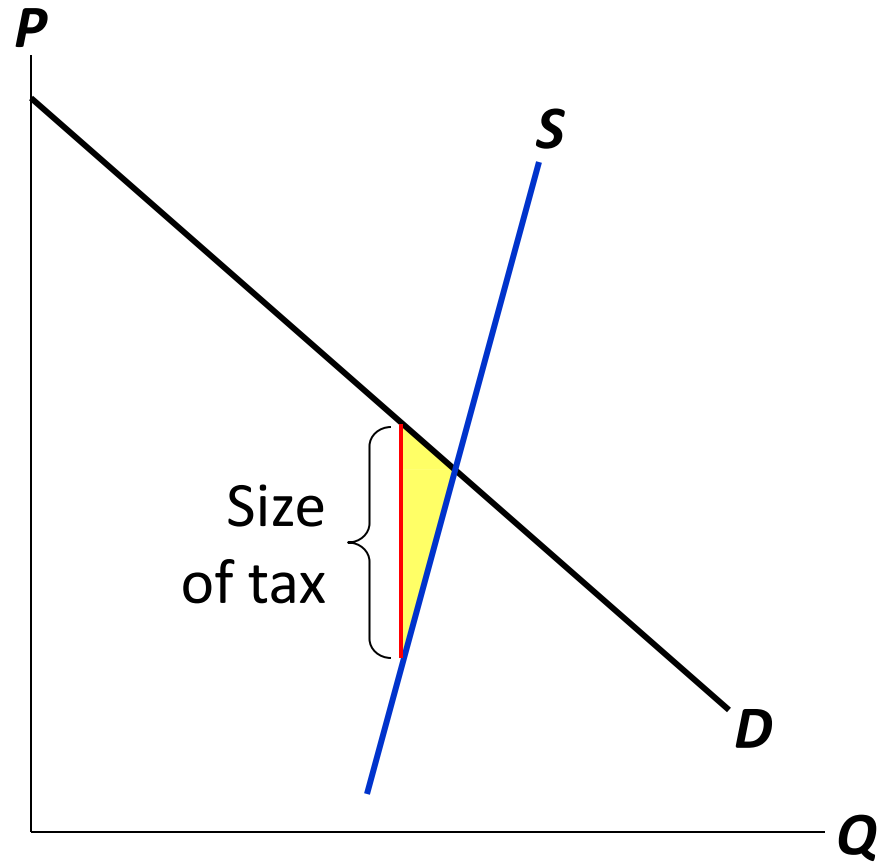


# What Determines the Size of the DWL?

- The govt needs tax revenue to finance roads, schools, police, etc., so it must tax some goods and services.
- Which ones? One answer is that govt should tax the goods or services with the smallest DWL.
- So when is the DWL small vs. large? Turns out it depends on the elasticities of supply and demand.
- Recall: The price elasticity of demand (or supply) measures how much quantity demanded (or supplied) changes when the price changes.

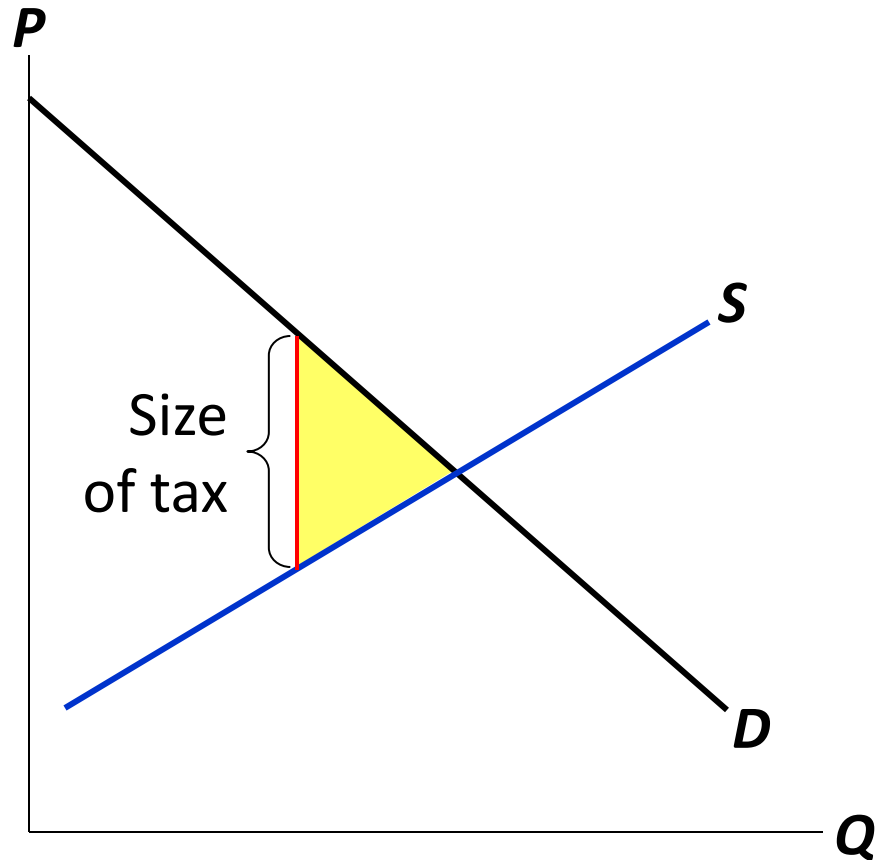
# DWL and the Elasticity of Supply

When supply is inelastic, the DWL of a tax is small.



# DWL and the Elasticity of Supply

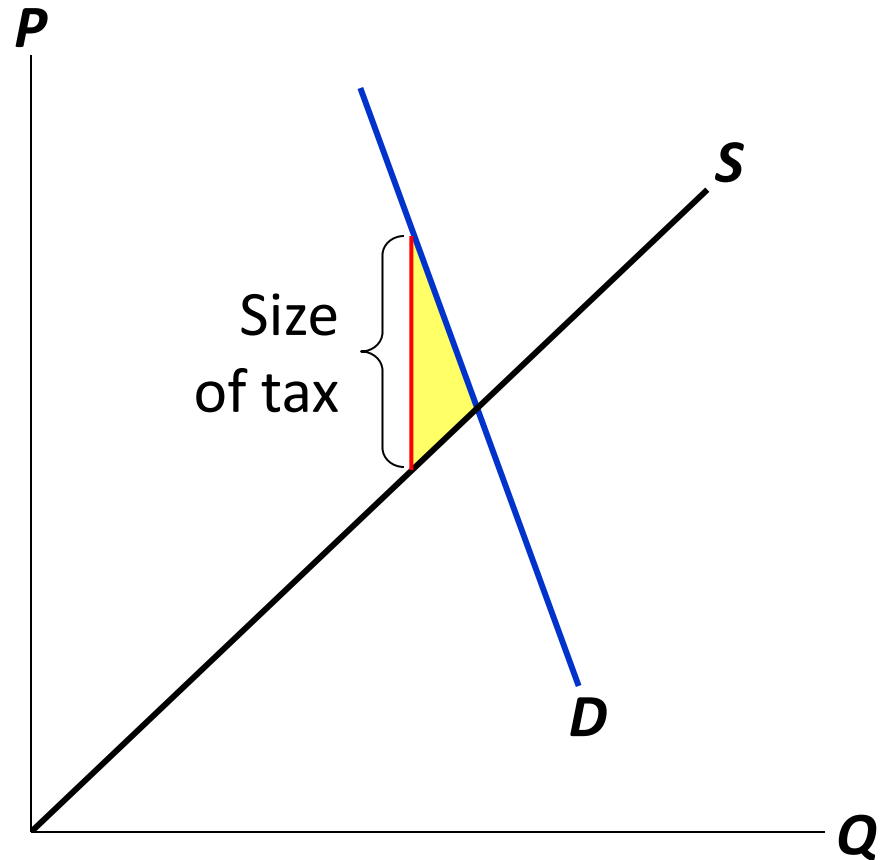
The more elastic  
is supply,  
the larger is  
the DWL.





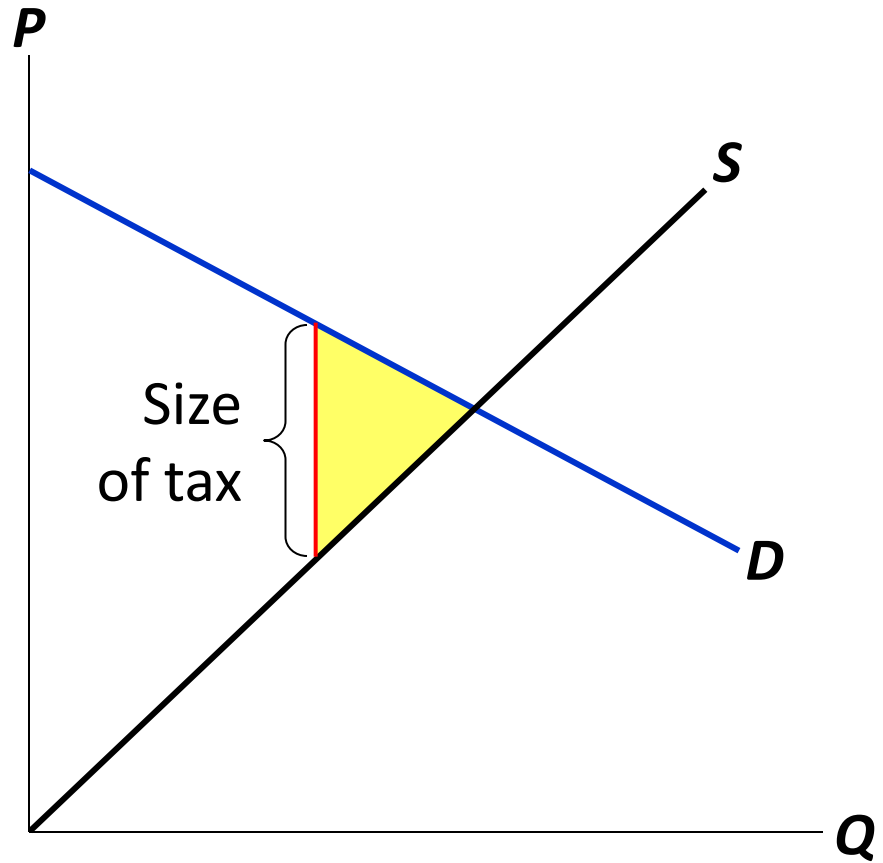
# DWL and the Elasticity of Supply

When demand is inelastic,  
the DWL of a tax  
is small.



# DWL and the Elasticity of Supply

The more elastic  
is demand,  
the larger is  
the DWL.



# Why Elasticity Affects the Size of DWL

- A tax distorts the market outcome: consumers buy less and producers sell less, so eq'm  $Q$  is below the surplus-maximizing quantity.
- Elasticity measures how much buyers and sellers respond to changes in price, and therefore determines how much the tax distorts the market outcome.

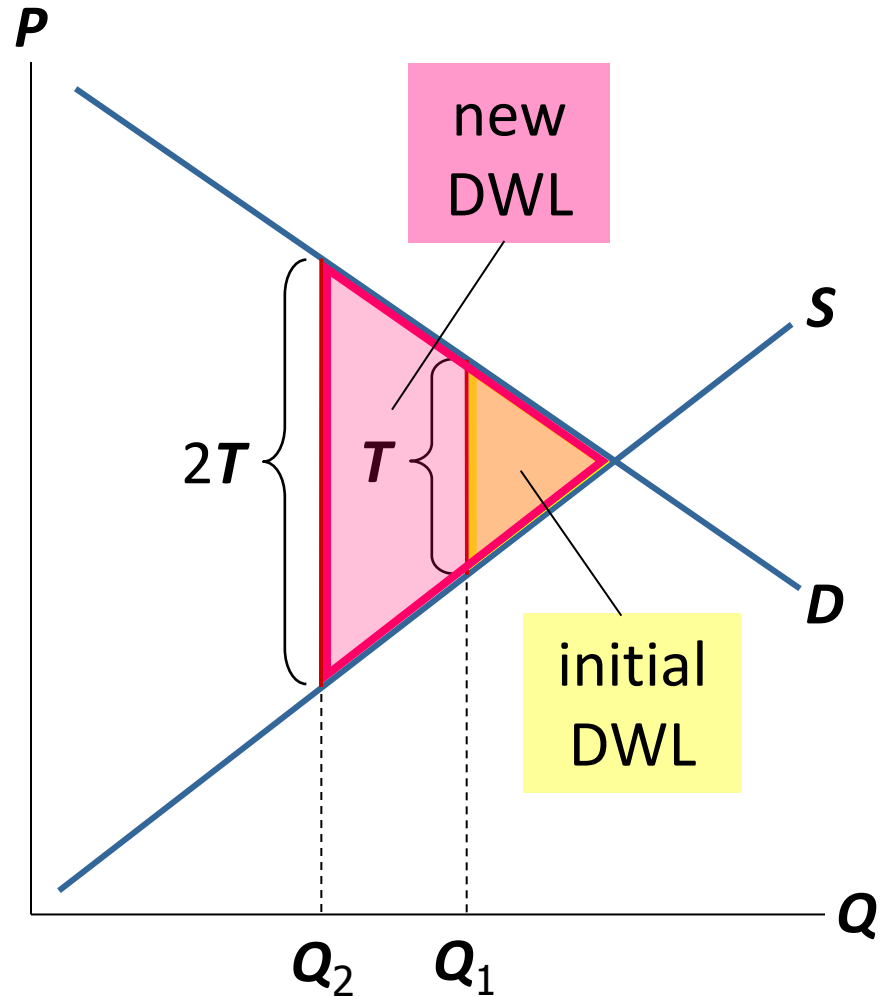
# The Effects of Changing the Size of the Tax

- Policymakers often change taxes, raising some and lowering others.
- What happens to DWL and tax revenue when taxes change? We explore this next....

# DWL and the Size of the Tax

Initially, the tax is  $T$  per unit.

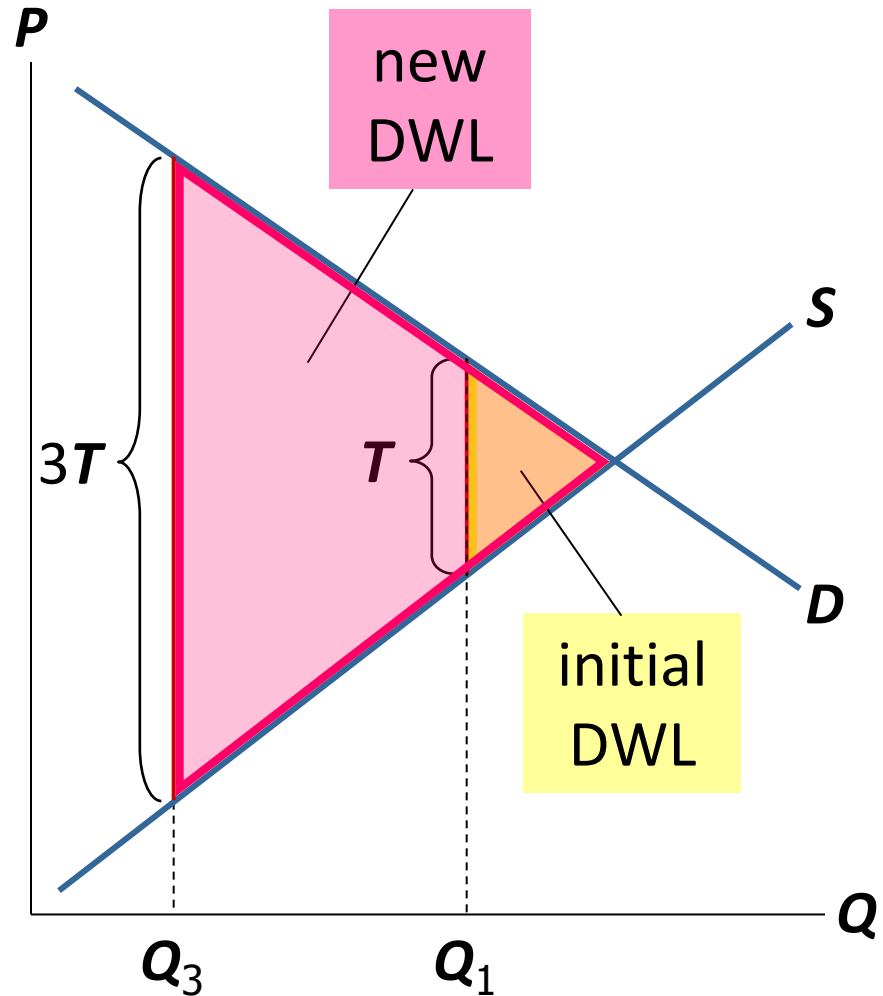
Doubling the tax causes the DWL to more than double.



# DWL and the Size of the Tax

Initially, the tax is  $T$  per unit.

Tripling the tax causes the DWL to more than triple.



# DWL and the Size of the Tax

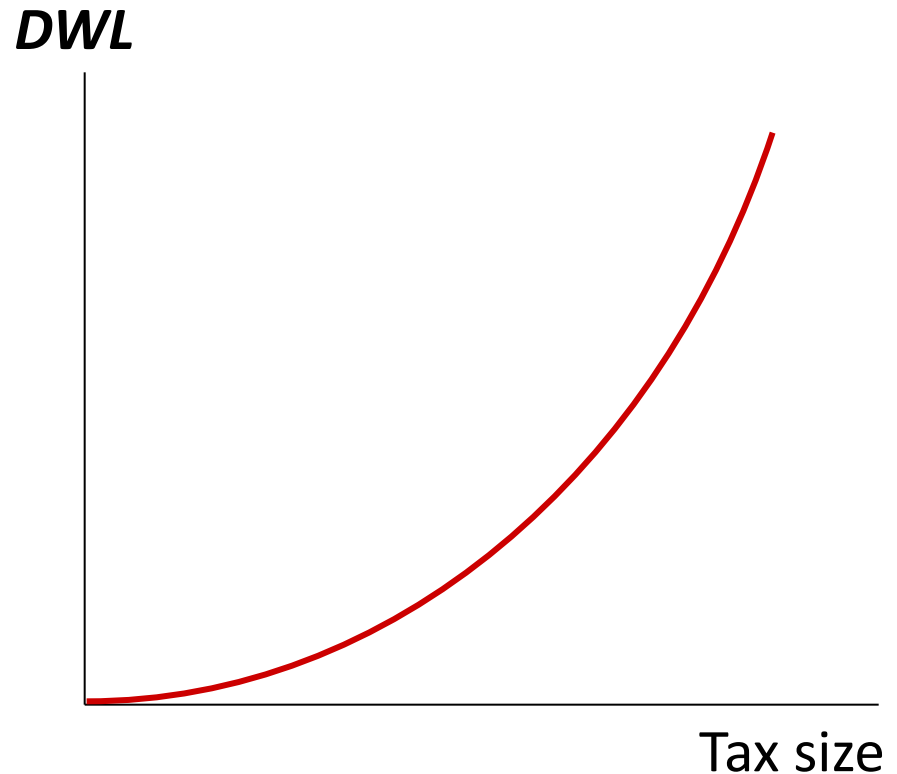
## Implication

*When tax rates are low, raising them doesn't cause much harm, and lowering them doesn't bring much benefit.*

*When tax rates are high, raising them is very harmful, and cutting them is very beneficial.*

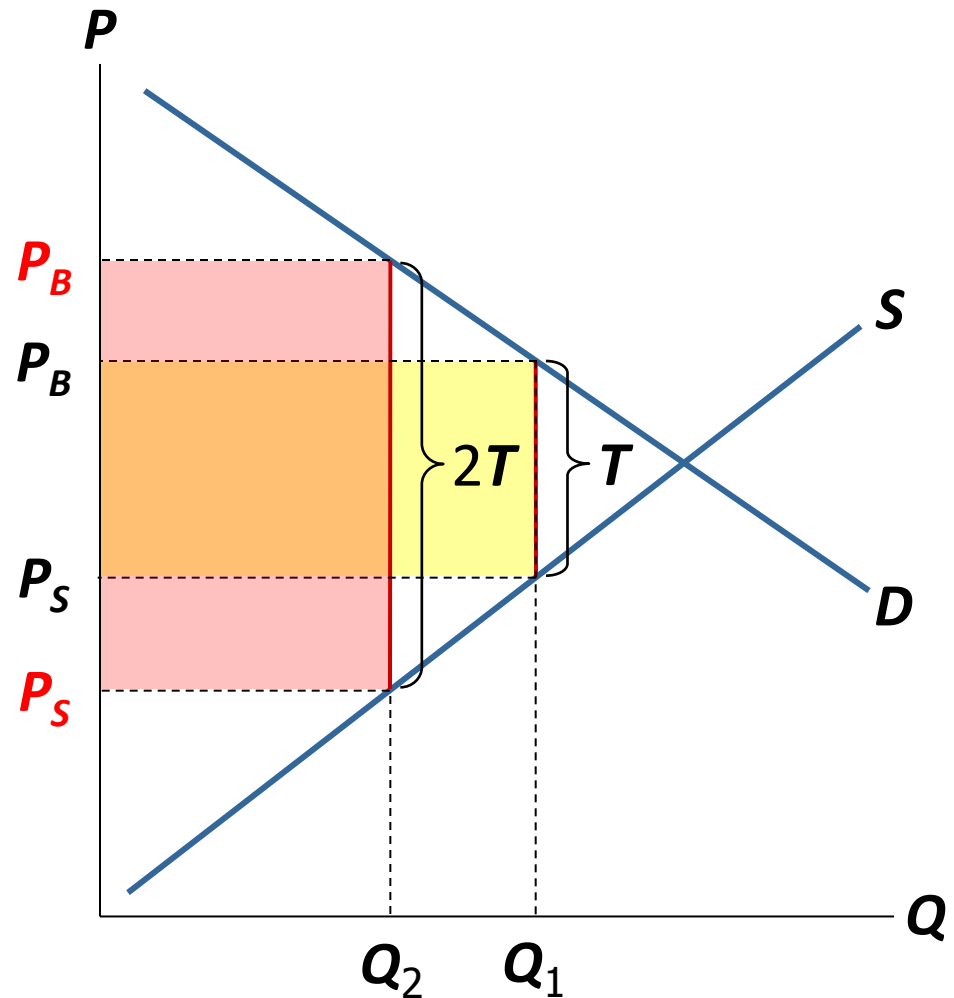
## Summary

*When a tax increases, DWL rises even more.*



# Revenue and the Size of the Tax

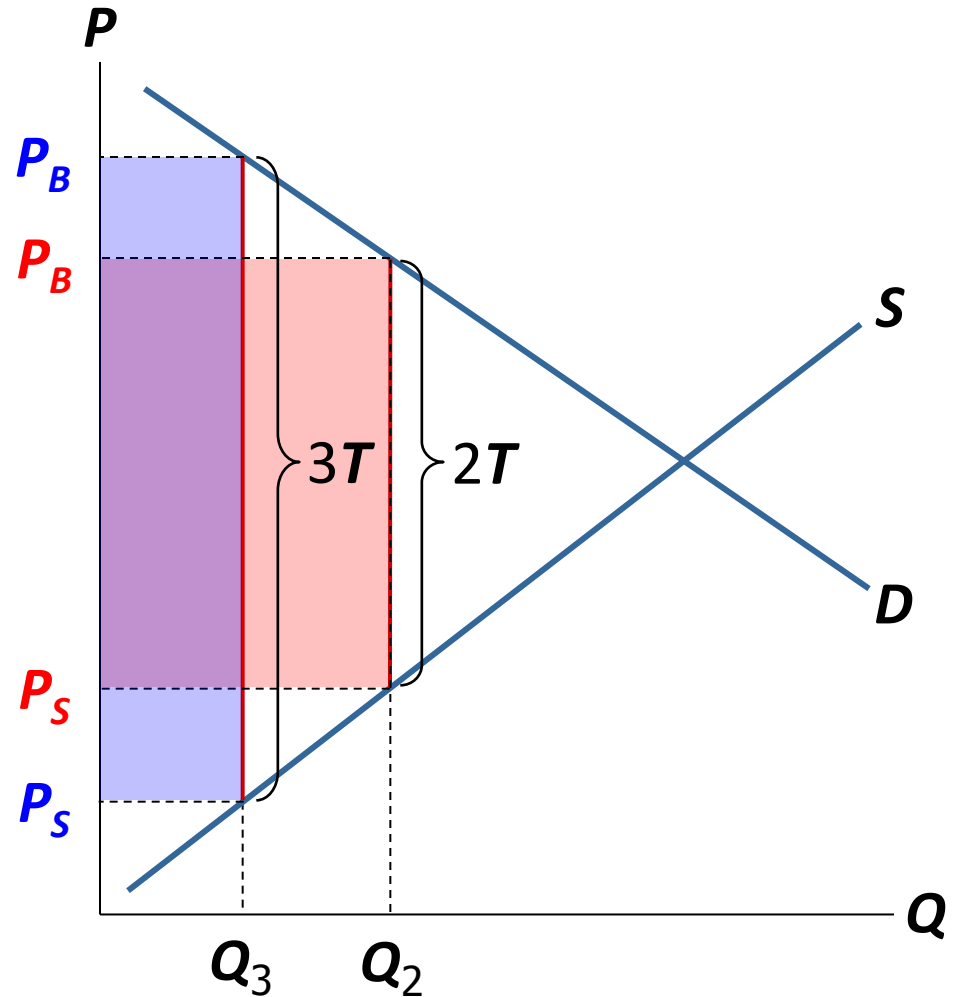
When the tax is small, increasing it causes tax revenue to rise.





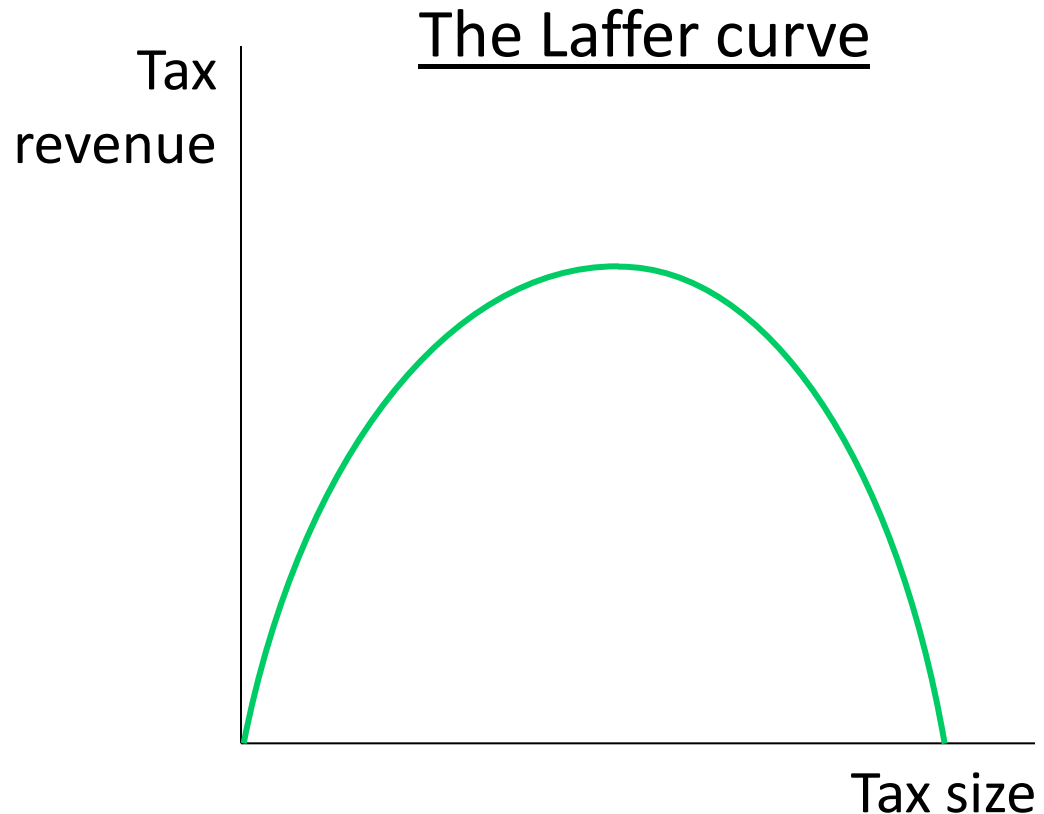
# Revenue and the Size of the Tax

When the tax is larger, increasing it causes tax revenue to fall.



# Revenue and the Size of the Tax

The **Laffer curve** shows the relationship between the size of the tax and tax revenue.



# CHAPTER SUMMARY

- A tax on a good reduces the welfare of buyers and sellers. This welfare loss usually exceeds the revenue the tax raises for the govt.
- The fall in total surplus (consumer surplus, producer surplus, and tax revenue) is called the deadweight loss (DWL) of the tax.
- A tax has a DWL because it causes consumers to buy less and producers to sell less, thus shrinking the market below the level that maximizes total surplus.

# CHAPTER SUMMARY

- The price elasticities of demand and supply measure how much buyers and sellers respond to price changes. Therefore, higher elasticities imply higher DWLs.
- An increase in the size of a tax causes the DWL to rise even more.
- An increase in the size of a tax causes revenue to rise at first, but eventually revenue falls because the tax reduces the size of the market.